Evaluation of a moderate resolution imaging spectroradiometer triangle-based algorithm for evapotranspiration estimates in subalpine regions

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Abstract. The current study evaluates the application of a moderate resolution imaging spectroradiometer (MODIS) triangle-based method to estimate evapotranspiration (ET) in subalpine environments. Topographic corrections and improved soil moisture representation are applied to a previously developed net radiation ($R_n$) model and triangle algorithm to develop an 8-day average ET product based solely on satellite products. We evaluate modeled $R_n$ and MODIS ET (MOD-ET) against ground-based values at four sites in the Sierra Nevada of northern California and also present a comparison between two monthly distributed ET datasets [operational simplified surface energy balance (SSEBop) and MODIS MOD16]. Modeled daily $R_n$ results indicate a systematic underestimation (between $-83$ and $-110 \text{ W/m}^2$ bias). Consequently, $R_n$ is bias-corrected before calculating MOD-ET. MOD-ET validation shows correlations between 0.15 and 0.45 with errors between 73 and $126 \text{ W/m}^2$. MOD-ET and SSEBop ET report correlations of 0.36 and 0.20, respectively, on average, compared to ground-based monthly ET. MOD16 underestimates monthly totals, with bias values on the range of $-14$ to $-144 \text{ W/m}^2$. Semiarid conditions and scale differences between the MODIS pixel and station contribute to errors with respect to observation. Overall, MOD-ET provides reasonable ET estimates and may better capture temporal dynamics in environments undergoing chronic disturbance. © The Authors. Published by SPIE under a Creative Commons Attribution 3.0 Unported License. Distribution or reproduction of this work in whole or in part requires full attribution of the original publication, including its DOI. [DOI: 10.1117/1.JRS.10.016002]

Keywords: evapotranspiration; triangle method; moderate resolution imaging spectroradiometer; semiarid; subalpine; evaporative fraction.

1 Introduction

Evapotranspiration (ET) is a key variable of study within multiple disciplines, including hydrology, meteorology, agriculture, and climate change science. ET governs the water cycling and energy transport among the biosphere, atmosphere, and hydrosphere and contributes largely to the prediction and estimation of regional-scale hydrologic processes, large-scale atmospheric circulation, and global climate change. The accurate characterization of ET flux across spatial and temporal scales is critical, especially in arid and semiarid environments where water deficiency may cause economic and political stress and constraints on sustainable development.

ET remains one of the most challenging hydrologic components to estimate as it depends on various climatological parameters such as temperature, solar radiation, wind speed, and vapor pressure, and also physical soil properties, land cover, and heterogeneity of the surrounding environment. Conventional ground-based measurement techniques, such as pan estimates, weighing lysimeters, eddy covariance systems, and the Bowen ratio system, are well-established methods for observing energy fluxes between the land surface and atmosphere. However, these...
techniques are point measurements with relatively small footprints that rarely exceed 1 to 2 km. These traditional ground-based systems provide accurate estimates over constrained, homogeneous areas, but are not capable of representing ET dynamics over large heterogeneous areas. Alternatively, satellite remote sensing is recognized as a viable means to acquire large-scale distributed data in a globally consistent and economically feasible manner due to its expansive global coverage, frequent estimates, and various spatial and temporal resolutions.

A number of models with varying complexity have been developed to estimate regional ET by combining remote sensing observations with ancillary surface and atmospheric data. These models include mapping ET at high resolution with internalized calibration, surface energy balance algorithm for land, simplified surface energy balance (SSEB) and its operationally applied byproduct SSEBop, and temperature–vegetation indices ($T_s$–VI) triangular and trapezoidal methods. Due to its simplicity, the $T_s$–VI triangle method has been widely used as a practical means to provide a regional parameterization of ET. The triangle approach is based on the derivation of an evaporative fraction (EF) using primarily satellite-derived surface parameters and limited ground-based measurements.

The $T_s$–VI triangle method uses a triangular or trapezoidal domain created when $T_s$ is plotted with VI and assumes a full range of soil moisture availability and fractional vegetation cover. The domain is characterized by two physical bounds: the upper dry (warm) and lower wet (cold) edges that represent limiting cases of soil moisture and EF by varying vegetation cover. The $T_s$–VI triangle relationship has been applied successfully in the study of soil moisture, land use, and drought monitoring. Since its introduction, the triangle method has undergone numerous modifications to derive regional ET estimates without ancillary data. Regardless of the modification, the general approach assumes that variations in surface temperature, from maxima to minima for a given vegetation index, are due to evaporative cooling effects rather than elevation variations. Consequently, a majority of studies have applied the triangle method over uniform topography, focusing on the effects of varying vegetation cover, spatial domain size, and climate.

The current study investigates the robustness of the triangle methodology for application in subalpine regions. An ET model by Kim and Hogue was successfully applied in southern Arizona and consists of a combination of the triangle method developed by Jiang and Islam and an improved interpolation method of the distribution of day and night land surface temperature (LST) difference developed by Wang et al. The approach by Kim and Hogue is novel due to its sole use of moderate resolution imaging spectroradiometer (MODIS) remote-sensing data to estimate $R_n$, ground heat flux, and EF (through the $T_s$–NDVI spatial distribution). In the current study, we apply two variations to the framework outlined in Kim and Hogue. First, thermal inertia information from the MODIS sensor is corrected for terrain-induced angular effects through the cosine method. Second, the $T_s$–VI triangular domain is interpreted through a modified two-step interpolation scheme that (1) assumes nonlinearity between the Priestley–Taylor parameter and vegetation indices and (2) assumes the Priestley–Taylor parameter ranges from 0 to (slope of saturated vapor pressure + psychrometric constant) / slope of saturated vapor pressure. The objectives of the current work are to test the performance of the modified Kim and Hogue MODIS ET framework for its suitability in subalpine regions and evaluate its performance relative to common distributed ET products, the MODIS-based MOD16 (MOD16), and the operational simplified surface energy balance (SSEBop).

2 Study Area

The Sagehen Creek watershed is located 32 km north of Truckee, California on the eastern slope of the northern Sierra Nevada (Fig. 1). The aspect, elevation, and slope in the selected area range from 0 deg to 360 deg, 1870 to 2650 m (2125 m on average), and 0 deg to 37 deg (8.0 deg on average), respectively (Fig. 2). Larger slopes correlate with higher elevations for all aspects, with an overall increase in slope with elevation [Fig. 2(d)]. Most of the area (77%) is located below a 2200-m elevation, and less than 3% of area is higher than 2500 m [Fig. 2(e)]. More than 93% of the area has a slope less than 15 deg, with sites located on and immediately surrounded by flat terrain (slope < 6 deg) [Fig. 2(a)]. The climate is characterized by dry summers with moderate
temperatures (3°C to 24°C) and wet winters with cooler temperatures (−8°C to 7°C). The most common forms of precipitation are light to moderate snow, light rain, and occasional summer thunderstorms. A majority of the precipitation occurs as snow (~85%), which accounts for 512 of the 590 mm of annual average total precipitation. Vegetation consists largely of evergreen forest (89%), with shrub-land scattered throughout (11%).

Fig. 1 Sagehen Creek watershed with study site locations 1, 3, 8, and 11 marked as circles. Elevation contours within the watershed are 100 m.

Fig. 2 Frequency of (a) slope, (b) aspect, (c) elevation, and (d) the change in slope with elevation for north, east, south, and west aspects.
3 Data

3.1 Ground-Based Evapotranspiration and Net Radiation
The Sagehen watershed includes weather stations that provide wind speed, short wave radiation, air temperature, and relative humidity; here, we focus on sites 1, 3, 8, and 11 (Table 1). These parameters are used to mathematically estimate net radiation through parameterization schemes outlined in Brutsaert, and ET using the Food and Agriculture Organization (FAO) Penman–Monteith standardization calculation of reference ET (ET$_0$) (see Appendix for details). Reported ET$_0$ at each site is set as the standardized crop ET for short crop, with the crop coefficient designated as the grass reference value during midgrowing season. Reported ET$_0$ values at each site are scaled by a soil stress coefficient ($K_s$) following FAO procedures to estimate actual ET (see Appendix for details). Additional measures are taken to confirm reliability by replacing tenuous data points (magnitudes greater than antecedent and subsequent data points) and missing data points with data points of no value. This ET is then aggregated to an 8-day daytime average ET and a total monthly ET product.

3.2 Moderate Resolution Imaging Spectroradiometer Satellite Observations
MODIS provides unprecedented high-quality landscape to global-scale land observations, as well as information regarding vegetation and surface energy, which are critical to the development of a remotely sensed ET model. A total of 10 variables obtained from MODIS atmospheric and land surface products are used in the MODIS ET (MOD-ET) model by Kim and Hogue and utilized in this study (Table 2). A combination of these variables is used to estimate $R_n$, ground-heat flux, and EF for the development of an 8-day and monthly ET product.

All MODIS products are acquired from the NASA Reverb ECHO site in the standard hierarchical data format between June and October of 2010 to 2014. Eight-day composite (MYD11A2) LST products have 1 km spatial resolution, which include daytime and nighttime products used to calculate the difference between daytime and nighttime LST. Air temperature ($T_a$) is back-calculated using an interpolated ratio between air temperature from MYD07 data and surface temperature from MYD06 based on Kim and Hogue. Actual (blue-sky) albedo (MCD43B3) is estimated using a solar zenith angle equal to solar noon and an optical depth of 0.2 based on a known black-and-white sky albedo. Due to the optimization of enhanced vegetation index (EVI) in improving the vegetation signal and reducing soil background influence, we substitute EVI in the algorithm in place of normalized difference vegetation index (NDVI). EVI is obtained through both terra (MOD13Q1) and aqua (MYD13Q1) platforms. Each product provides a 16-day composite dataset with a 250-m spatial resolution and phasing of both terra and aqua generates a combined 8-day time series of vegetation indices. The highest spatial resolution (250 m) based on MOD13Q1 and MYD13Q1 is used for the final spatial resolution of the proposed MOD-ET product. MODIS products with coarser resolution (1 to 5 km) are resampled to a 250-m resolution.

<table>
<thead>
<tr>
<th>Site number</th>
<th>Latitude (deg)</th>
<th>Longitude (deg)</th>
<th>Elevation (m)</th>
<th>Available ET (n) (8-day period)</th>
<th>Slope (deg)</th>
<th>Aspect (deg)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Site 1</td>
<td>39.431</td>
<td>−120.240</td>
<td>1940</td>
<td>86</td>
<td>4.29</td>
<td>163.83</td>
</tr>
<tr>
<td>Site 3</td>
<td>39.427</td>
<td>−120.283</td>
<td>2130</td>
<td>48</td>
<td>4.29</td>
<td>62.58</td>
</tr>
<tr>
<td>Site 8</td>
<td>38.418</td>
<td>−120.239</td>
<td>2080</td>
<td>47</td>
<td>2.49</td>
<td>331.50</td>
</tr>
<tr>
<td>Site 11</td>
<td>39.435</td>
<td>−120.288</td>
<td>2110</td>
<td>17</td>
<td>5.38</td>
<td>143.97</td>
</tr>
</tbody>
</table>
4 Methodology

The modified 8-day, 250 m MOD-ET product is evaluated for sites 1, 3, 8, and 11 between June and October from 2010 to 2014. First, we compare $R_n$ estimates derived from an MODIS-based algorithm against ground-based $R_n$ estimates. Second, we evaluate $R_n$ bias-corrected MOD-ET to ground-based ET to estimate potential error in our interpretation of the $T_s - EVI$ domain. Following the $R_n$ bias-corrected MOD-ET analysis, we compare MOD-ET estimates with those derived without topographic correction. Finally, we compare MOD-ET values to MOD16 and SSEBop between June and October from 2010 to 2013.

4.1 Moderate Resolution Imaging Spectroradiometer-Based Triangle Evapotranspiration Algorithm

4.1.1 Estimation of available radiant energy ($R_n - G$)

A satellite-based (MODIS) stand-alone methodology, initially developed by Kim and Hogue, is utilized for the estimation of $R_n$. The methodology builds upon previous algorithms and equations to equate upward and downward short- and long-wave radiation under both clear and cloudy sky conditions. The $R_n$ model developed in Kim and Hogue incorporates the Paulescu and Schlett model to determine instantaneous downward shortwave radiation under clear-sky conditions. However, the current study implements Eq. (5) as suggested by Bisht and Bras, along with a regional parameterization scheme from the Kim and Hogue methodology that requires no regional calibration. We also substitute the cloud product from MYD08 with the cloud product from MYD06.

Table 2  Summary of MODIS products used in this study with relevant spatial and temporal information.

<table>
<thead>
<tr>
<th>Product name</th>
<th>Layer</th>
<th>Grid resolution (km)</th>
<th>Temporal resolution</th>
</tr>
</thead>
<tbody>
<tr>
<td>MYD03</td>
<td>Solar zenith angle</td>
<td>1 x 1</td>
<td>Daily (daytime)</td>
</tr>
<tr>
<td></td>
<td>Geolocation</td>
<td>1 x 1</td>
<td>Daily (daytime)</td>
</tr>
<tr>
<td>MYD05_L2</td>
<td>Water vapor</td>
<td>1 x 1</td>
<td>Daily (daytime)</td>
</tr>
<tr>
<td>MYD06_L2</td>
<td>Cloud fraction</td>
<td>5 x 5</td>
<td>Daily (daytime)</td>
</tr>
<tr>
<td></td>
<td>Cloud optical thickness</td>
<td>1 x 1</td>
<td>Daily (daytime)</td>
</tr>
<tr>
<td></td>
<td>Surface temperature</td>
<td>5 x 5</td>
<td>Daily (daytime)</td>
</tr>
<tr>
<td>MYD07_L2</td>
<td>Total ozone</td>
<td>5 x 5</td>
<td>Daily (daytime)</td>
</tr>
<tr>
<td></td>
<td>Air temperature</td>
<td>5 x 5</td>
<td>Daily (daytime)</td>
</tr>
<tr>
<td></td>
<td>Dew-point temperature</td>
<td>5 x 5</td>
<td>Daily (daytime)</td>
</tr>
<tr>
<td>MYD11_L2</td>
<td>Emissivity</td>
<td>1 x 1</td>
<td>Daily (daytime)</td>
</tr>
<tr>
<td></td>
<td>LST</td>
<td>1 x 1</td>
<td>Daily (daytime)</td>
</tr>
<tr>
<td>MOD13Q1b</td>
<td>EVI</td>
<td>250 x 250</td>
<td>16 days</td>
</tr>
<tr>
<td>MYD13Q1a</td>
<td>EVI</td>
<td>250 x 250</td>
<td>16 days</td>
</tr>
<tr>
<td>MCD43B3ab</td>
<td>Albedo</td>
<td>1 x 1</td>
<td>8 days</td>
</tr>
<tr>
<td>MYD11A1a</td>
<td>LST</td>
<td>1 x 1</td>
<td>Daily (daytime)</td>
</tr>
<tr>
<td>MYD11A2a</td>
<td>LST</td>
<td>1 x 1</td>
<td>8 days (daytime/nighttime)</td>
</tr>
</tbody>
</table>

aMODIS aqua satellite.
bMODIS terra satellite.
The upward longwave radiation for clear sky is expressed using the Stefan–Boltzmann equation

\[ R_l \uparrow_{\text{clear}} = \varepsilon_s \sigma T_s^4, \quad (1) \]

where \( \varepsilon_s \) is the surface emissivity, \( \sigma \) is the Stephan–Boltzmann constant (5.67 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4} \), and \( T_s \) is the surface temperature (K) (MYD11).

Downward longwave radiation for a clear sky is based on a parameterization scheme by Brutsaert\(^47\) and is estimated as

\[ R_l \downarrow_{\text{clear}} = \varepsilon_a \sigma T_a^4, \quad (2) \]

where \( \varepsilon_a \) is the air emissivity [determined by water vapor pressure (MYD05) and air temperature] and \( T_a \) is the interpolated air temperature (K) (MYD07).

Downward longwave radiation for cloudy pixels is estimated through a proposed methodology by Bisht and Bras\(^46\) and can be expressed as

\[ R_l \downarrow_{\text{cloudy}} = \varepsilon_a \sigma T_a^4 + (1 - \varepsilon_a) \varepsilon_c \sigma T_c^4, \quad (3) \]

where \( T_a \) is interpolated air temperature, \( \varepsilon_c \) is cloud emissivity (MYD11), and \( T_c \) is the cloud temperature (MYD06).

Under cloudy conditions, upward longwave radiation\(^6\) is estimated as

\[ R_l \uparrow_{\text{cloudy}} = \varepsilon_{sA} \sigma T_{sA}^4, \quad (4) \]

where the surface temperature \( (T_{sA}) \) is obtained from MYD06, and surface emissivity \( (\varepsilon_{sA}) \) is obtained from MYD11A2.

Estimation of downward shortwave radiation under clear sky conditions stems from Zillman\(^48\) and modifications by Bisht and Bras.\(^46\) This parameterization scheme uses near-surface vapor pressure \( (e_0) \) (MYD07 and MYD05) and solar zenith angle \( (\theta) \) (MYD03) to estimate downward shortwave radiation as follows:

\[ R_s \downarrow_{\text{clear}} = \frac{S_0 \cos^2(\theta)}{1.085 \cos(\theta) + e_0[2.7 + \cos(\theta)] \times 10^{-3} + \beta}, \quad (5) \]

where \( S_0 \) is the solar constant at the top of the atmosphere (1367 W/m\(^2\)). Niemelä et al.\(^49\) and Bisht et al.\(^50\) have shown that a \( \beta \) value of 0.1 corresponds to overestimation of downward shortwave radiation and have alternatively proposed a \( \beta \) value of 0.2, which is used in the current study.

Downward shortwave radiation under cloudy conditions is estimated as a linear combination of the fluxes from clear sky and cloudy sky\(^46\) and weighted by cloud fraction, as developed by Slingo\(^51\)

\[ R_s \downarrow_{\text{cloudy}} = R_s \downarrow_{\text{clear}} \left[ (1 - N) + Ne^{-e_0 \tau} \right], \quad (6) \]

where \( N \) is the cloud cover fraction (MYD06), \( \tau \) is the cloud optical thickness (MYD06), and \( \theta \) is the solar zenith angle (MYD03).

Using Eqs. (1)–(6), we estimate an instantaneous \( R_n \) under all sky conditions using Eq. (7) as proposed by Kim and Hogue\(^6\)

\[ R_n = (1 - A_0)R_s \downarrow + R_l \downarrow - R_l \uparrow, \quad (7) \]

where \( A_0 \) is surface albedo. Instantaneous net radiation estimates are then converted to daily average \( R_n \) estimates [Eq. (8)] through a sinusoidal function, which assumes \( R_n \) values become positive at sunrise and begin to decline during sunset\(^49,50,52\)

\[ R_{n \text{ daily}} = R_n \uparrow \frac{2}{\pi \sin \left( \frac{\theta_{\text{sunrise}} - \theta_{\text{sunset}}}{\theta_{\text{sunrise}} - \theta_{\text{sunset}}} \pi \right)}, \quad (8) \]
where $R_{n\text{daily}}$ and $R_{n\text{i}}$ are daily and instantaneous $R_n$, respectively, $t_{\text{sunrise}}$, and $t_{\text{sunset}}$ are sunrise and sunset times obtained from the US Naval Observatory and $t_i$ is the satellite over-pass time.

Estimation of soil heat flux ($G_0$) is achieved through a proposed methodology by Bastiaanssen,\textsuperscript{15} which utilizes a radiometric surface temperature product, surface albedo, and NDVI. Bastiaanssen\textsuperscript{15} computes soil heat flux empirically, by considering the effects of surface heating, soil moisture, and intercepted solar radiation

$$G_0 = R_n \left( \frac{T_{\text{TMI}}}{A_0} \right) \frac{(0.0038A_0 + 0.0074A_0^2)(1 - 0.98\text{EVI}^4)}{1 - 0.98\text{EVI}^4},$$

where $T_{\text{TMI}}$ (°C) is the radiometric surface temperature, $A_0$ is the surface albedo, and EVI is the enhanced vegetation index (MOD13Q1 and MYD13Q1). In the current study, $T_{\text{TMI}}$ is estimated from MYD11, and albedo is estimated through the combined MODIS terra and aqua MCD43B3.

### 4.1.2 Estimation of evaporative fraction

EF is the ratio of latent heat flux (LE) to available radiant energy [Eq. (10)]. We utilize a modified methodology proposed by Kim and Hogue\textsuperscript{6} that employs the Wang et al.\textsuperscript{22} model to derive EF and calculate the standard deviation. Maximum temperature differences exceeding one standard

$$EF = \frac{\text{LE}}{R_n - G} = \frac{\Delta}{\Delta + \gamma},$$

where LE is representative of ET (W/m\textsuperscript{2}), $R_n$ is the net radiation (W/m\textsuperscript{2}), $G$ is the soil heat flux (W/m\textsuperscript{2}), $\gamma$ is the psychrometric constant (hPa/K), $\alpha$ is the Priestley–Taylor parameter accounting for aerodynamic and canopy resistances, and $\Delta$ is the slope of saturated vapor pressure at air temperature (hPa/K), which can be calculated as

$$\Delta = \frac{26297.77}{(T_a - 29.65)} \exp \left[ \frac{17.67(T_a - 273.15)}{T_a - 29.65} \right].$$

Due to a less than 5% difference between the use of air and surface temperatures\textsuperscript{22} and an instability of air temperature retrieval from MYD07\textsuperscript{5}, acquired surface temperatures from the MYD11 product are used to estimate $\Delta$ rather than air temperature.\textsuperscript{19,22,44} Surface temperatures are then corrected for terrain-induced angular effects through the cosine method\textsuperscript{12,33} as follows:

$$T = \left( \frac{T_s^4}{\cos \gamma} \right)^{1/4}.$$

where $T$ is the corrected LST, $T_s$ is the satellite-derived LST, and $\gamma$ is the angle between the satellite-view path and the normal to the terrain element.\textsuperscript{33} For a thermal band, the angle of emitted radianc can be geometrically determined by

$$\cos \gamma = \cos \omega \cos \delta + \sin \omega \sin \delta \cos (\varphi_s - \varphi),$$

where $\omega$ is the local slope angle, $\delta$ is the satellite zenith angle, $\varphi_s$ is the satellite azimuth angle, and $\varphi$ is the aspect angle of the terrain element.

Prior to estimating EF, both dry and wet edges in the $\Delta T$ – EVI trapezoidal domain must be determined. In the current study, the wet edge is interpreted as a constant temperature line set as the minimum temperature difference.\textsuperscript{19,22} The warm edge of the trapezoidal space is estimated by establishing constant intervals of EVI and finding the maximum temperature difference associated with each interval. Assuming a linear decrease in temperature with increasing EVI,\textsuperscript{4,6,18-22} we develop a linear regression model based on the acquired maximum temperature differences and calculate the standard deviation. Maximum temperature differences exceeding one standard
deviation from the linear regression model are considered outliers and omitted. The new set of maximum temperatures is used to redevelop the linear regression model to obtain the final dry edge and subsequently the associated maximum and minimum temperature difference.

The Priestley–Taylor parameter, $\alpha$ [Eq. (10)] for each pixel ($i$) is determined using a two-step nonlinear interpolation scheme from the $T_s – \text{EVI}$ trapezoidal domain. First, the value of $\alpha$ corresponding to the driest bare soil pixel (no vegetation and temperature is at a maximum) is set to 0 ($\alpha_{\text{min}} = 0$). Next, the value of $\alpha$ corresponding to maximum vegetation on the wet edge (maximum amount of vegetation and temperature is at a minimum) is set to $(\Delta + \gamma / \Delta$) $[\alpha_{\text{max}} = (\Delta + \gamma / \Delta)]$. The value of $\alpha$ for pixel ($i$) is estimated by determining $\alpha_{\text{min}, i}$ by assuming that $\alpha_{\text{min}, i}$ varies nonlinearly with EVI between $\alpha_{\text{min}}$ and $\alpha_{\text{max}}$.

\[
\alpha_{\text{min}, i} = \alpha_{\text{max}, i} \left( \frac{\text{EVI}_i - \text{EVI}_{\text{min}}}{\text{EVI}_{\text{max}} - \text{EVI}_{\text{min}}} \right)^2.
\]

(14)

Having established the upper and lower bounds of $\alpha$, the $\alpha_i$ for any pixel with an EVI and $\Delta T$ is determined by

\[
\alpha_i = \frac{\Delta T_{\text{max}} - \Delta T_i}{\Delta T_{\text{max}} - \Delta T_{\text{min}}} (\alpha_{\text{max}} - \alpha_{\text{min}}) + \alpha_{\text{min}}.
\]

(15)

Finally, substituting $\alpha_i$ from Eq. (15) into Eq. (10), we estimate EF for any pixel within the boundary of the triangular domain as

\[
\text{EF} = \frac{\Delta}{\Delta + \gamma} \left[ \frac{\Delta T_{\text{max}} - \Delta T_i}{\Delta T_{\text{max}} - \Delta T_{\text{min}}} (\alpha_{\text{max}} - \alpha_{\text{min}}) + \alpha_{\text{min}} \right].
\]

(16)

where $\Delta T_{\text{max}}$ and $\Delta T_{\text{min}}$ are the corresponding maximum and minimum surface temperature differences (8-day composite) at the dry and wet edges, respectively, for a given EVI (8-day composite). Lastly, an 8-day ET product is derived using Eq. (17), estimated $R_n$ [Eq. (8)], estimated soil heat flux ($G_0$) [Eq. (9)], and EF [Eq. (16)] assuming a constant EF throughout a day.

\[
\text{ET} = \text{EF}(R_n - G).
\]

(17)

4.2 Operational Evapotranspiration Products

Modeled ET estimates are compared against ground-based ET to evaluate the performance of the global MODIS ET datasets (MOD16A2 monthly) and SSEBop.

4.2.1 MODIS MOD16 ET (MOD16)

Global MODIS ET datasets (MOD16A2) are obtained from the University of Montana’s Numerical Terradynamic Simulation Group and are available at spatial resolution of 1 km for the entire global vegetated land surface for 8-day, monthly, and annual time intervals. The original MOD16 algorithm, based on the Penman–Monteith equation, has been modified to consider both the surface energy portioning process and atmospheric drivers on ET. The algorithm uses a range of MODIS products, including land cover, albedo, leaf area index, and EVI. Additionally, the algorithm requires daily meteorological data inputs for regional and global ET mapping and monitoring, which are obtained from NASA’s Global Modeling and Assimilation Office. In the current study, we use 1 km, monthly MODIS MOD16 ET datasets between June and October from 2010 to 2013.

4.2.2 Operational simplified surface energy balance

SSEBop is an MODIS-based ET dataset based on SSEB that uses model assimilated weather datasets and MODIS thermal images to produce values for the contiguous United States at 8-day,
SSEBop introduces a new simplified parameterization to estimate an actual ET value using predefined boundary conditions that are unique to each pixel for the “hot” and “cold” reference conditions. ET is then estimated as a function of LST obtained from remotely sensed data and reference ET from global weather datasets using the SSEB approach. The original SSEB formulation is enhanced with a lapse rate correction factor, significantly improving the influence of topography on surface temperature.

Furthermore, Senay et al. address both elevation and latitude effects on surface temperature using an LST/air temperature difference rather than exclusively surface temperature. Because the boundary for hot and cold reference conditions are predefined for each location and period using a simplified climatological energy balance calculation procedure, remotely sensed LST is the only specification required by the user to estimate ET fractions, simplifying SSEBop simulation. In the current study, we utilize the 1 km, monthly SSEBop ET generated between June and October of 2010 to 2013. SSEBop ET data are acquired through the US geological survey geo data portal.

5 Results and Discussion

5.1 Validation of Net Radiation

We first evaluate the MOD-ET algorithm $R_n$ values with ground-based $R_n$. The comparison between daily ground-based $R_n$ and daily MOD-ET $R_n$ has root mean square error (RMSE) ranging from 106 to 132 W/m$^2$ and correlation coefficients between 0.67 and 0.80 for all sites (Fig. 3). There is also consistent model underestimation at each site, with bias values ranging from $-83$ to $-110$ W/m$^2$ (Fig. 3). The observed negative biases trends are consistent with Kim and Hogue, who report bias from $-102$ to $-46$ W/m$^2$. Kim and Hogue also report RMSE between 69 and 122 W/m$^2$, with correlation coefficients ranging from 0.65 to 0.69. Bisht and Bras report RMSE values and correlations of 41 W/m$^2$ and 0.88, respectively; while Tang et al. report RMSE values and correlations of 57 to 84 W/m$^2$ and 0.34 to 0.50, respectively.

Fig. 3 Observed $R_n$ and MODIS-derived $R_n$ at each site (labeled in the bottom right) with correlation coefficient ($R$), RMSE, percent bias, and bias. The dashed line represents a one-to-one correlation, while the solid line is the linear regression of the data.
Our results show a negative bias of ∼25% on average between the sites. Correlations are similar or slightly better than recent studies and are attributed to the longer time period in the current study. Systematic underestimation of surface $R_n$ may stem from unsatisfactory performance of the shortwave radiation scheme used in the study. Kim and Hogue report between −17% and −22% bias in instantaneous shortwave radiation, with RMSE errors as high as 226 W/m² when incorporating the shortwave radiation scheme. The current study finds similar trends (not shown) when comparing daily average observed shortwave radiation and modeled shortwave radiation, with bias values between −33 and −36 W/m² and RMSE errors of 192 W/m² on average between the sites. Furthermore, it is important to note the significant uncertainty that may arise from the scale differences present when comparing an MODIS pixel to the *in situ* data. Several inputs, such as MYD06 and MYD07, are coarse (1 to 5 km) and may not capture subtle terrain or canopy differences present at the tower sites, adding uncertainty and reducing accuracy. Although there is a slight increase in RMSE at all sites, the daily $R_n$ estimates presented in this section are fairly similar to those reported in the literature, while having the added advantage of being available under all sky conditions and requiring no ground-based observations.

### 5.2 Evaluation of Derived Evapotranspiration

#### 5.2.1 MOD-ET versus ground-based observations

Evaluation of MOD-ET against ground-based estimated ET is undertaken for all four study sites between the months of June and October for years 2010 to 2014. We derive new ET values based on bias-corrected $R_n$ estimates. Bias-corrected ET estimates provide a thorough analysis of the derivation of EF from the $\Delta T_s$ − EVI domain as we are unable to directly compare observed EF to modeled EF. Lastly, we derive ET values without topographic correction (cosine method) to determine the sensitivity of the triangle method to variations in slope, aspect, and elevation.

Bias-corrected MOD-ET estimates at sites 1, 3, and 11 show positive bias (67.0, 88.7, and 84.9 W/m², respectively), while site 8 reports a moderately positive bias at 15.3 W/m². RMSE errors and correlations range between 73.3 and 126.0 W/m² and 0.15 and 0.45 between all sites, respectively. Results from site 11 have relatively poor results that are attributed to the minimal, 17, 8-day periods of available data (84.9, 126, and 0.15 for bias, RMSE, and correlation, respectively). Sites 1, 3, and 8 record 86, 48, and 47 8-day periods of available data, respectively (Table 1). RMSE errors reported here (Fig. 4 and Table 3) are larger than those reported by Kim and Hogue, with lower correlations at all sites except site 1 (Fig. 4 and Table 3).

Similar overestimation of modeled ET is reported by Kim and Hogue at two sites characterized as having minimal soil moisture availability. However, the implementation of their triangle method under riparian or sufficient soil water content conditions shows improved performance. Prior to ET comparison, Kim and Hogue evaluated EF derived from the triangle method against observed EF, which demonstrate that the performance of the triangle method suffered under water-stressed conditions, leading to overestimations of EF and subsequently ET. Tang et al. also note significant overestimations of EF when applying an MODIS triangle-based ET method over two flux tower sites in southern Arizona. Additionally, Wang et al. report that EF values remain nonuniform under low soil moisture content, regardless of the vegetation uniformity.

Kim and Hogue report systematically underestimated $R_n$ values and overestimated ET from soil moisture limited sites. When comparing our originally derived MOD-ET product, which also utilizes slightly underestimated $R_n$ values, we find much improved bias values (27.1, 41.8, 25.2, and 31.4 W/m² for sites 1, 3, 8, and 11, respectively). This is likely due to the non-linear formulation of the $\Delta T_s$ − EVI space used in the current study, which has been shown to produce lower EF estimates when compared to the linear formulation by improving moisture availability interpretation within the $\Delta T_s$ − EVI domain. Because estimates of EF and $R_n$ are independent from one another, we are able to bias correct $R_n$ and relate errors in ET to the EF. As previously mentioned, $R_n$ bias-corrected MOD-ET shows moderate overestimations of ET (EF) when applied over water-stressed regions (Fig. 4), which is similar to observations by Kim and Hogue and Tang et al. Despite improved bias when comparing originally derived MOD-ET
estimates to values reported in Kim and Hogue,6 Rn bias-corrected MOD-ET estimates suggest that calculated EF from the $\Delta T_s - \text{EVI}$ domain under water-stressed conditions remains an issue. MOD-ET calculated without topographic correction show minimal variation compared to those reported using the topographic correction. All sites have a percent difference in correlation between 1.4% and 3.7%, with correlations decreasing for all sites. Sites 1, 3, 8, and 11 report a percent difference in RMSE of 7.2, 8.2, −4.5, and 4.8 W/m$^2$, respectively. Changes in bias are also relatively small when omitting topographic correction, with sites 1, 3, and 11 reporting an increase of 8.7 W/m$^2$ on average, where site 8 reports a decrease of 8.3 W/m$^2$. Given that slope has a stronger influence on ET than elevation,63 minute changes in MOD-ET estimates

**Table 3** RMSE and $R$ values for triangle-based ET from recent relevant studies.

<table>
<thead>
<tr>
<th>Study</th>
<th>Site</th>
<th>$R$ (unit less)</th>
<th>RMSE (W/m$^2$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Tang et al.31</td>
<td>Audubon Ranch</td>
<td>0.47</td>
<td>45.4</td>
</tr>
<tr>
<td></td>
<td>Kendall Grassland</td>
<td>0.68</td>
<td>36.8</td>
</tr>
<tr>
<td>Wang and Jia62</td>
<td>Average between all 14 sites</td>
<td>0.57</td>
<td>22.0</td>
</tr>
<tr>
<td>Kim and Hogue6</td>
<td>Kendall</td>
<td>0.43</td>
<td>33.0</td>
</tr>
<tr>
<td></td>
<td>Charleston</td>
<td>0.85</td>
<td>48.0</td>
</tr>
<tr>
<td></td>
<td>Lewis Spring</td>
<td>0.86</td>
<td>32.0</td>
</tr>
<tr>
<td></td>
<td>Santa Rita</td>
<td>0.69</td>
<td>45.0</td>
</tr>
<tr>
<td>MOD-ET (bias corrected)</td>
<td>1</td>
<td>0.43</td>
<td>88.1</td>
</tr>
<tr>
<td></td>
<td>3</td>
<td>0.22</td>
<td>111.0</td>
</tr>
<tr>
<td></td>
<td>8</td>
<td>0.45</td>
<td>73.3</td>
</tr>
<tr>
<td></td>
<td>11</td>
<td>0.15</td>
<td>126.0</td>
</tr>
</tbody>
</table>
from topographic correction are likely associated with the relatively flat surface of the watershed. Despite an elevation range between 1900 and 2600 m, 93% of the watershed has a slope less than 15 deg, with sites located on and immediately surrounded by flat terrain (slope < 6 deg) [Fig. 2(a)].

The average annual ET response to elevation and slope for different aspect angles over the Sagehen basin is also highlighted (Fig. 5). Years 2010 to 2012 show an expected increase in ET with elevation, with peak values occurring between roughly 2050 and 2200 m, before steadily decreasing at elevations greater than 2300 m [Figs. 5(a), 5(c), 5(e), and 5(g)]. Marginal variability between aspect angles is attributed to the frequency of smaller slopes [Fig. 2(a)], dampening the effects aspect may have on ET estimation. However, we note ET values for the south-facing slopes are lower than those for the north-, east-, and west-facing slopes. This trend is most prominent between 2100 and 2300 m for years 2011 and 2013 [Figs. 5(c) and 5(g)]. South-facing slopes receive more direct sunlight, heating the surface, and possibly enhancing the turbulent mixing of the near surface air mass. Consequently, the increase in $R_n$ is repartitioned into sensible heat, causing a decrease in the latent heat flux and available moisture for ET, which is similar to Zhao and Liu$^{63}$ and Gao et al.$^{64}$ Specifically, Zhao and Liu$^{63}$ reported ET values for south-facing slopes are lower than north-facing slopes, while Gao et al.$^{64}$ indicated that ET for south-facing woodland and grassland sites tended to decrease with increasing elevation.

In addition to slope and slope aspect, trends in ET with elevation may also be attributed to the soil moisture and vegetation properties at specific elevations.$^{6,8,19-21,26,65,66}$ Mean summer season EVI with elevation trends closely follow those of ET, with lower EVI values (0.47 to 0.50) at the lowest elevations in the basin (1880 to 2000 m) (Fig. 6). Peak EVI values (0.52 to 0.53) occur around 2100 m (Fig. 6), coinciding with peak ET values (Fig. 5). EVI values then decrease from ~0.50 to 0.40 from 2100 m in elevation to 2600 m (Fig. 6), similar to overall trends in ET (Fig. 5).

Similar to our modeled $R_n$ underestimation, bias between MOD-ET and ground-based ET may be attributed to the discrepancy between spatial scales of the satellite imagery and surface stations. Ground-based measurements are influenced by observation height,$^8$ canopy structure,
and other local environmental factors. Therefore, it is a changing variable on both space and time scales, while a satellite measurement with fixed pixel size is characterized as a static constant (incapable of deciphering small-scale heterogeneity). Additional factors contributing to observed biases include uncertainties from instrumental measurements and remote-sensing retrievals.

5.2.2 Distributed evapotranspiration comparison

ET estimates derived during this study are further evaluated through a comparison to global MODIS ET datasets (MOD16A2) and SSEBop. Results show considerable underestimation of MOD16 monthly ET across all sites, with bias values between −14.0 and −84.4 mm/month (Table 4 and Fig. 7) when compared to ground-based estimates. SSEBop shows slightly improved bias, with a large range between −3.8 and −113.0 mm/month (Table 4). Focusing on site 1, which has the largest available ground-based ET dataset, we find that MOD-ET overestimates monthly totals during all months (June, July, August, September, and October). SSEBop and MOD16 produce a systematic underestimation of monthly total ET, while matching the overall pattern of observed data (correlations of 0.39 and 0.36, respectively) (Fig. 7). However, MOD16 monthly total estimates are considerably lower than those reported by SSEBop and MOD-ET, with slightly improved bias at site 8 when compared to SSEBop. Due to the unavailability of ground-based ET datasets at the subsequent sites, we cannot further assess the degree of success of MOD-ET as compared to MOD16 and SSEBop. Despite the lack of available ground-based ET estimates, a clear pattern in the magnitude of estimated monthly ET is evident.

Table 4 RMSE, correlation (R), and bias values of MOD-ET, MOD16, and SSEBop monthly total ET products compared against observed.

<table>
<thead>
<tr>
<th>Site</th>
<th>RMSE (mm/month)</th>
<th>R (unit less)</th>
<th>Bias (mm/month)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>MOD-ET</td>
<td>MOD16</td>
<td>SSEBop</td>
</tr>
<tr>
<td>1</td>
<td>87.5</td>
<td>93.0</td>
<td>51.6</td>
</tr>
<tr>
<td>3</td>
<td>158.0</td>
<td>81.2</td>
<td>64.9</td>
</tr>
<tr>
<td>8</td>
<td>42.8</td>
<td>152.0</td>
<td>127.0</td>
</tr>
<tr>
<td>11</td>
<td>199</td>
<td>60.6</td>
<td>69.8</td>
</tr>
</tbody>
</table>

Fig. 6 Summer season mean EVI response to elevation for years 2010 to 2013 over the Sagehen basin.
total ET is presented, with MOD-ET producing the largest monthly total ET estimates, followed in magnitude by SSEBop and MOD16.

Focusing on site 1 (as done previously), we find SSEBop and MOD-ET estimates display a substantial improvement in overall performance compared to MOD16 estimates. The poor performance of MOD16 can be attributed to both elevation and climate. Velpuri et al. report a decrease in MOD16 ET accuracy with increasing elevation, as well as a negative bias in more arid, steppe, and cold region climates. Velpuri et al. also demonstrate that SSEBop does not decrease in accuracy with increasing elevation, which is attributed to the enhanced algorithm by Senay et al. Velpuri et al. also note better agreement in SSEBop over climate zones covering most of the western United States. Trends seen in Velpuri et al. are similar to those observed in our MOD-ET, with similar topography, vegetation, and relative climate at the high elevation sites making for a reasonable comparison.

6 Summary and Conclusions

The current work investigates the robustness of a stand-alone MODIS-based ET product for all sky conditions, with a focus on a subalpine basin. The evaluated method provides a simple and direct estimate of ET, without the need for ground-based meteorological data and shows the potential for monitoring ET in regions where little to no gauged data exists. The approach is tested at four sites (sites 1, 3, 8, and 11) within the Sagehen Creek watershed in the northern Sierra Nevada.

The $R_n$ model used in this study systematically underestimates net radiation at all sites, with bias values ranging from $-83$ to $-110$ W/m$^2$. Similar trends are reported by Kim and Hogue and may be the result of a shortwave radiation scheme used in the current algorithm.

Originally derived MOD-ET 8-day estimates show relatively strong correlation and minimal bias at all sites when compared to ground-based measurements. Improved bias under increased water stress is likely attributed to a nonlinear decomposition, allowing for a better representation of available soil moisture. Net radiation bias-corrected 8-day ET estimates are slightly overestimated at all sites with bias values between 15 and 89 W/m$^2$. Despite improved bias...
when comparing originally derived MOD-ET estimates, the $R_n$ bias-corrected MOD-ET estimates suggest that estimating EF from the $\Delta T_s – \text{EVI}$ domain under water-stressed conditions remains an unresolved issue. This is attributed to the influence of the deeper root zone soil moisture on total ET in regions experiencing increased water stress. Although improved through a nonlinear decomposition, including a certain degree of water stress, the triangular relationship between LST and EVI still may not be able to correctly represent this deeper soil moisture available to plants.

Comparisons between topographically corrected MOD-ET and nontopographically corrected MOD-ET led to small variations in ET estimates. Reported changes in RMSE and bias from topographically corrected to nontopographically corrected ET estimates are 2.5 and 4.5 W/m², respectively, on average between the sites. Minor differences are associated with the relatively flat surface of the area directly surrounding all four sites (slope < 6 deg).

Additional uncertainty may result from the obvious scale differences between the MODIS-based value and the ground-based station. Heterogeneity within the MODIS pixel contributes to the error in ET due to the scale differences between the satellite and surface point measurement.

MOD16 ET significantly underestimates monthly totals, with bias values ranging from −13.9 to −144.0 W/m². Underestimation by MOD16 is likely attributed to the models decreasing accuracy in ET approximation with increasing elevation and reported negative bias in arid, steppe, and cold arid regions. However, comparisons made between the MOD-ET product and the SSEBop ET product with observed monthly total ET estimates show slightly improved results, with correlations between 0.58 and 0.39 for site 1, respectively.

Overall, the proposed MOD-ET model performs relatively well and results correspond with past studies and the current SSEBop model. Independence from ancillary data and near real-time applicability makes the MOD-ET suitable for monitoring ET in regions where little or no gauged data exists. We note that there are still significant challenges present in the estimation of actual ET in water-stressed type environments with complex topography and vegetative/soil moisture heterogeneity. However, the products utilized in the MOD-ET algorithm have the ability to reflect spatial and temporal dynamics from climate and land surface alteration. For example, the Sagehen Creek Experimental Forest is currently undergoing extensive forest thinning activities to reduce natural vegetation build-up and restore a healthy wildfire regime. Such activities will alter the land cover and ET dynamics. The ability to incorporate this MOD-ET product may enhance future hydrologic studies in this and other forested regions undergoing acute land use change.

### Appendix: Derivation of Ground-Based Net Radiation and ET

Ground-based net radiation is estimated according to

$$R_n = R_s(1 - A_0) + \varepsilon_s R_l \downarrow - R_l \uparrow,$$

where $R_s$ is the shortwave radiation (provided at the site) (W/m²), $A_0$ is the albedo of the surface (unitless), $\varepsilon_s$ is the surface emissivity (unitless), and $R_l \downarrow$ and $R_l \uparrow$ are downward and upward longwave radiation (W/m²), respectively. $A_0$ and $\varepsilon_s$ are approximated as 0.25 and 0.97, respectively, after considering the vegetative properties at each site and comparing to corresponding natural surfaces as reported by Brutsaert. $R_l \uparrow$ is estimated according to the Stefan–Boltzmann equation as

$$R_l \uparrow = \varepsilon_s \sigma T_s^4,$$

where $\sigma$ is the Stephan–Boltzmann constant ($5.67 \times 10^{-8}$ W m⁻² K⁻⁴), and $T_s$ is the LST (K). $R_l \downarrow$ for all sky conditions is approximated by first calculating $R_l \downarrow$ under clear sky conditions [Eq. (20)]

$$R_l \downarrow = \varepsilon_{ac} \sigma T_a^4,$$

where $\varepsilon_{ac}$ is defined as the atmospheric emissivity under clear skies and can be written as
where $e_a$ is the vapor pressure of air (hPa), and $a$ and $b$ are constants derived to be 1.24 and 1/7 under average conditions that represent a standard atmosphere.\(^{68-70}\) $Rl$ for all sky conditions is then estimated by

$$RI \downarrow = RI \, I_{cl\,\,\text{air}} \left(1 + a_1 f_C^b \right),$$

where $f_C$ is the fractional cloudiness and $a_1$ and $b_1$ are 0.0496 and 2.45, respectively, derived from Sugita and Brutsaert.\(^{71}\)

The standardized FAO Penman–Monteith ET equation is intended to simplify and clarify the presentation and application of the method and is expressed as

$$ET_0 = \frac{0.408 \Delta (R_n - G) + \gamma \frac{C_a}{T - 273} u_2 (e_a - e_s)}{\Delta + \gamma (1 + C_d u_2)},$$

where $ET_0$ is the reference ET (mm $\cdot$ d$^{-1}$), $R_n$ is the calculated net radiation at the crop surface (MJ m$^{-2}$ $\cdot$ d$^{-1}$), $G$ is the soil heat flux density at the soil surface (MJ m$^{-2}$ $\cdot$ d$^{-1}$), $T$ is the mean daily or hourly air temperature ($^\circ$C), $u_2$ is the mean daily wind speed at 2 m height (ms$^{-1}$), $e_s$ is the saturation vapor pressure (kPa), $e_a$ is the mean actual vapor pressure (kPa), $\Delta$ is the slope of the saturation vapor pressure–temperature curve (kPa$\cdot$°C$^{-1}$), $C_a$ is the numerator constant that changes with reference type and calculation time step (K mm$^3$ Mg$^{-1}$ d$^{-1}$), and $C_d$ is the denominator constant that changes with reference type and calculation time step (s m$^{-1}$). The 0.408 coefficient has units of m$^2$ mm MJ$^{-1}$. The reference surface used in the estimation of ET is expressed as a short crop (similar to clipped grass).

Actual ET, denoted by $ET_{act}$, is calculated as

$$ET_{act} = K_s K_c ET_0,$$

where $K_s$ is the soil stress coefficient (0 to 1.0), $K_c$ is the crop coefficient (determined to be 1.0),\(^{38}\) and $ET_0$ is the reference ET reported at each site. $K_s$ is given by

$$K_s = \frac{TAW - D_r}{TAW - RAW},$$

where TAW is the total available soil water in the root zone (mm), RAW is the readily available soil water in the root zone (mm), and $D_r$ is root zone depletion (mm). The total available water is estimated as the difference between water content at field capacity and wilting point,\(^{38}\) and is expressed as

$$TAW = 1000 (\theta_{fc} - \theta_{wp}) z_r,$$

where $z_r$ is the maximum rooting depth (m). Readily available water of the root zone is estimated as

$$RAW = p(TAW),$$

where $p$ is the fraction of TAW that a crop can extract from the root zone without experiencing stress.\(^{38}\) Following FAO-56 procedures, $p$ is estimated as 0.49, while $z_r$, $\theta_{fc}$, and $\theta_{wp}$ are determined to be 2.0 m,\(^{72-74}\) 0.33,\(^{75}\) and 0.13,\(^{75}\) respectively. Following the calculations of TAW and RAW, root zone depletion is estimated as

$$D_r = 1000 (\theta_{fc} - \theta_l) z_r,$$

where $\theta_l$ is the average soil water content in the active rooting depth for a given day. Daily average soil water content estimates at each site (depth of 40 to 100 cm) are acquired through the national land data assimilation model (NOAH) output. If the root zone depletion for a given
day is less than or equal to RAW, $K_s$ is equal to 1.0 and no stress is induced on the plant. When root zone depletion is greater than RAW, $K_s$ varies from 0 to 1 and is used to scale reported reference ET to actual ET under water-stressed conditions. Additional information pertaining to the FAO-56 procedure can be found in Allen et al.\textsuperscript{38}

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